lengths of $\mathrm{O}-\mathrm{H} \cdots \mathrm{O}$ bonds range from $2 \cdot 621(4)$ to $3.056(4) \AA$ and $\mathrm{N}-\mathrm{H} \cdot \mathrm{O}$ from $2 \cdot 828(4)$ to $3 \cdot 379(5) \AA$.

Table 10. Hydrogen-bonding parameters

| Symmetry code |  |  |  |
| :--- | ---: | ---: | ---: |
| (I) | $x$, | $y$, | $z ;$ |
| (II) | $-x$, | $-y$, | $-z ;$ |
| (III) | $-x$ | $\frac{1}{2}+y$, | $\frac{1}{2}-z ;$ |
| (IV) | $x$ | $\frac{1}{2}-y$, | $\frac{1}{2}+z ;$ |
| (V) | $x-1$, | $\frac{1}{2}-y$, | $-\frac{1}{2}+z ;$ |
| (VI) | $-x$ | $-\frac{1}{2}+y$, | $\frac{1}{2}-z ;$ |
| (VII) | $-x+1$, | $-y$, | $-z+1 ;$ |
| (VIII) | $-x$, | $-y, z+1 ;$ |  |
| (IX) | $x$ | $\frac{1}{2}-y$, | $z-\frac{1}{2} ;$ |
| (X) | $-x+1$, | $\frac{1}{2}+y$, | $\frac{1}{2}-z ;$ |

Distance between bonded atoms ( $\AA$ )

| $\mathrm{N}\left(1^{1}\right)-\mathrm{H}\left(1^{1}\right)-\mathrm{O}\left(4^{\mathrm{v}}\right)$ | 2.828 (4) |
| :---: | :---: |
| $\mathrm{N}\left(1^{1}\right)-\mathrm{H}\left(2^{1}\right)-\mathrm{O}\left(5^{\mathrm{VI}}\right)$ | $2 \cdot 886$ (4) |
| $\mathrm{N}\left(1^{1}\right)-\mathrm{H}\left(4^{\text {l }}\right.$ )--O(8) | 2.979 (5) |
| $\mathrm{N}\left(1^{1}\right)-\mathrm{H}\left(4^{\text {l }}\right.$ )--O(9 ${ }^{\text {r }}$ ) | $2 \cdot 887$ (5) |
| $\mathrm{N}\left(1^{1}\right)-\mathrm{H}\left(3^{1}\right)-\mathrm{O}\left(10^{\text {III }}\right)$ | 3.087 (4) |
| $\mathrm{N}\left(1^{1}\right)-\mathrm{H}\left(3^{1}\right)-\mathrm{O}\left(11^{1}\right)$ | 3.097 (4) |
| $\mathrm{N}\left(2^{1}\right)-\mathrm{H}\left(6^{1}\right)-\mathrm{O}\left(9^{1}\right)$ | $3 \cdot 096$ (5) |
| $\mathrm{N}\left(2^{1}\right)-\mathrm{H}\left(6^{1}\right)-\mathrm{O}\left(9^{111}\right)$ | 3.379 (5) |
| $\mathrm{N}\left(2^{1}\right)-\mathrm{H}\left(5^{1}\right)-\mathrm{O}\left(11^{1}\right)$ | 3.016 (5) |
| $\mathrm{N}\left(2^{1}\right)-\mathrm{H}\left(7^{\text {l }}\right)-\mathrm{O}\left(4^{\text {VII }}\right.$ ) | 3.003 (6) |
| $\mathrm{N}\left(2^{\mathrm{l}}\right)-\mathrm{H}\left(8^{1}\right)-\mathrm{O}\left(7^{\text {IV }}\right.$ ) | 2.893 (5) |
| $\mathrm{N}\left(2^{\text {I }}\right)-\mathrm{H}\left(8^{\prime}\right)-\mathrm{O}\left(11^{\text {VIII }}\right.$ ) | $3 \cdot 104$ (5) |
| $\mathrm{O}\left(2^{\mathrm{l}}\right)-\mathrm{H}\left(11^{\mathrm{r}}\right)-\mathrm{O}\left(5^{\text {1x }}\right.$ ) | $2 \cdot 685$ (4) |
| $\mathrm{O}\left(2^{1}\right)-\mathrm{H}\left(12^{2}\right)-\mathrm{O}\left(3^{\mathrm{x}}\right)$ | 2.621 (4) |
| $\mathrm{O}\left(11^{1}\right)-\mathrm{H}\left(9^{1}\right)-\mathrm{O}\left(1^{\text {III }}\right)$ | 3.056 (4) |
| $\mathrm{O}\left(11^{1}\right)-\mathrm{H}\left(10^{\mathrm{I}}\right)-\mathrm{O}\left(6^{\mathrm{VI}}\right)$ | $2 \cdot 955$ (4) |

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# The Crystal Structure of Sodium Acetate Trihydrate 

By T.Stanley Cameron<br>University of Ulster, Coleraine, N. Ireland

and Kh. M. Mannan* and Md. Obaidur Rahman<br>Physics Department, Dacca University, Bangladesh

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The molecular structure of the title compound has been determined by direct methods from photographic data. $\mathrm{Na}^{+}\left(\mathrm{CH}_{3} \mathrm{COO}\right)^{-} .3 \mathrm{H}_{2} \mathrm{O}$, monoclinic, $a=12.475, b=10.407, c=10.449 \AA, \beta=112.65^{\circ}$, space group $C 2 / c, 475$ reflexions, $R=0 \cdot 11$. The $\mathrm{Na}^{+}$ion has distorted octahedral coordination with six oxygen atoms. Adjacent octahedra share an edge and form a continuous chain along the $z$ axis. Along the chain the separations between the $\mathrm{Na}^{+}$ions are 3.39 and $3.56 \AA$ and the $\mathrm{Na}{ }^{+}-\mathrm{O}$ distances are in the range $2.35-2.56 \AA$. The $\mathrm{C}-\mathrm{O}$ bond lengths are 1.23 and $1.31 \AA$ and both oxygen atoms are hydrogen bonded to two water molecules.

Sodium acetate trihydrate is one of the better known salts of one of the simple organic acids; as such its crystal structure has been determined.

[^0]
## Experimental

Crystals of sodium acetate trihydrate, grown by slow evaporation from aqueous solution, are small hexagons. Weissenberg and oscillation photographs established that the crystals were monoclinic in space
group $C 2 / c$ (Mannan \& Rahman, 1972) and not $C 2 / m$ as was reported by Padmanabhan (1952). The choice of space group $C 2 / c$ rather than $C c$ was borne out by the analysis and independently by the goniometric finding of the prismatic class (Groth, 1910). In this context the reported $a: b: c$ ratios are $1 \cdot 1809: 1: 0 \cdot 9962$ with $\beta=111.71^{\circ}$, while the ratios from the crystal data (below) are $1 \cdot 1987: 1: 1 \cdot 0040$ with $\beta=112 \cdot 65^{\circ}$. The discrepancy may in part be due to the different conditions in which the two sets of data were obtained (Groth gives no details but the X-ray data were determined in Dacca at $30^{\circ} \mathrm{C}$ and high humidity). However the X-ray cell parameters may be less accurate than their e.s.d.'s suggest.

## Crystal data

$\mathrm{C}_{2} \mathrm{H}_{3} \mathrm{NaO}_{2} .3 \mathrm{H}_{2} \mathrm{O}, \quad M=136 \cdot 08$, monoclinic, $a=$ 12.475 (2), $\quad b=10.407$ (3), $\quad c=10.449$ (3) $\quad \AA, \quad \beta=$ $112.65(5)^{\circ} . U=1251.94 \AA^{3}$, systematic extinctions $h k l: h+k=2 n+1, h 0 l: l=2 n+1$; space group $C 2 / c$ ( $C_{2 h}^{6}$, No. 15), $D_{m}=1.45$ (by flotation), $D_{c}=1.45$ $\mathrm{g} \mathrm{cm}^{-3}$ (for $\left.Z=8\right), F(000)=576, \mathrm{Cu} K \alpha(\lambda=1.54178 \AA)$ radiation, $\mu=18.3 \mathrm{~cm}^{-1}$, Weissenberg photographic data layers 0 kl to $11 \mathrm{kl}, 475$ reflexions significantly above the background intensity; an additional 81 reflexions too weak to measure were assigned half the value of the local minimum observable intensity. Lorentz and polarization but not absorption corrections were applied.

Attempts to solve the structure from Patterson functions in projection were unsuccessful and it was thought that several of the atoms were in special positions. The phases of 76 out of the 80 reflexions with the largest $E$ 's were determined by direct methods with the symbolic addition procedure. The resultant $E$ map showed the position of the $\mathrm{Na}^{+}$ion, the acetate group and two water molecules; also there were two peaks in the $E$ map on the twofold axis which were in chemically sensible positions to complete the coordination sphere about the $\mathrm{Na}^{+}$ion. An $F_{o}$ map was calculated for the trial structure without the two atoms in special positions from which the position of the two remaining atoms was confirmed.

The structure was refined by block-diagonal leastsquares calculations with the weighting scheme $w=1$ for $\left|F_{o}\right|_{\text {abs }}<30.0$ and $w=\left(30 \cdot 0 / F_{\text {oabs }}\right)^{2}$ for the remaining reflexions. After four cycles with individual isotropic
temperature factors on all atoms $R$ was 0.19 and this reduced to 0.15 after three cycles with anisotropic temperature factors for all the atoms in general positions. An electron density difference map calculated at this stage clearly indicated the position of all the nine hydrogen atoms and when these atoms were included (with $B=4 \AA^{2}$ ) but not refined in the structure-factor


Fig. 1. A projection of the structure viewed along c. Hydrogen bonds are shown as broken lines. All the labelled atoms are in equivalent position [1] (Table 2).
$\qquad$


Fig. 2. The sodium ion environment as seen down a. The subscript numbers refer to the equivalent positions in Table 2.

Table 1. Final atomic parameters $\left(\times 10^{4}\right)$
$U$ 's are in $\AA^{2}$. The temperature factor $T=\exp \left[-2 \pi^{2}\left(U_{11} h^{2} a^{* 2}+U_{22} k^{2} b^{* 2}+U_{33} l^{2} c^{* 2}+2 U_{23} k l b^{*} c^{*}+2 U_{13} h l a^{*} c^{*}+2 U_{12} h k a^{*} b^{*}\right)\right]$, and $W$ refers to the oxygen atom of a water molecule.

|  | $x$ | $y$ | $z$ | $U_{11}$ | $U_{22}$ | $U_{33}$ | $U_{23}$ | $U_{13}$ | $U_{12}$ |
| :--- | :---: | :---: | :--- | :--- | :--- | :--- | ---: | ---: | ---: |
| Na | $883(4)$ | $4287(4)$ | $4201(5)$ | 41 | 21 | 45 | -15 | 16 | -21 |
| $\mathrm{O}(1)$ | $2645(9)$ | $4652(8)$ | $3732(9)$ | 60 | 18 | 58 | -15 | 34 | -51 |
| $\mathrm{O}(2)$ | $3368(10)$ | $6539(9)$ | $3464(10)$ | 92 | 38 | 75 | -23 | 50 | 56 |
| $\mathrm{C}(1)$ | $3254(11)$ | $5597(11)$ | $4231(13)$ | 37 | 24 | 50 | -54 | 29 | -10 |
| $\mathrm{C} 2(2)$ | $3939(14)$ | $5684(14)$ | $5760(15)$ | 98 | 50 | 31 | 16 | -31 | 34 |
| $W(1)$ | $3493(10)$ | $2113(8)$ | $3821(10)$ | 86 | 22 | 56 | 8 | -26 | 13 |
| $W(2)$ | $8789(7)$ | $4171(7)$ | $4048(8)$ | 17 | 22 | 29 | 7 | -9 | 14 |

Table 1 (cont.)

|  | $r$ | $y$ | $B_{\text {iso }} *$ |  |
| :--- | ---: | :---: | :---: | :---: |
| $W(3)$ | 0 | $6002(8)$ | 2500 | $2 \cdot 553$ |
| $W(4)$ | 0 | $2608(9)$ | 2500 | $2 \cdot 102$ |
| H(1) | 4650 | 3800 | 800 | $4 \cdot 0$ |
| H(2) | 3300 | 4000 | 1200 | $4 \cdot 0$ |
| H(3) | 4000 | 5250 | 1000 | $4 \cdot 0$ |
| H(4) | 630 | 6500 | 2500 | $4 \cdot 0$ |
| H(5) | 730 | 2000 | 2500 | $4 \cdot 0$ |
| H(6) | 1870 | 8000 | 1250 | $4 \cdot 0$ |
| H(7) | 2300 | 6800 | 1750 | $4 \cdot 0$ |
| H(8) | 625 | 3250 | 250 | $4 \cdot 0$ |
| H(9) | 1867 | 4250 | 250 | $4 \cdot 0$ |
|  | $*$ |  |  |  |

Table 2. Key to the labelling of atoms
Equivalent position Label Equivalent position Label

| $x, y, r$ | $z$ | $[1]$ | $\frac{1}{2}+x, \frac{1}{2}+y, \frac{1}{2}+z$ | $[5]$ |
| :--- | :--- | :--- | :--- | :--- |
| $\bar{x}, \bar{y}$, | $\bar{z}$ | $[2]$ | $\frac{1}{2}-x, \frac{1}{2}-y, \frac{1}{2}-z$ | $[6]$ |
| $\bar{x}, y, \frac{1}{2}-z$ | $[3]$ | $\frac{1}{2}-x, \frac{1}{2}+y, \frac{1}{2}-z$ | $[7]$ |  |
| $x, \bar{y}, \frac{1}{2}+z$ | $[4]$ | $\frac{1}{2}+x, \frac{1}{2}-y, \frac{1}{2}+z$ | $[8]$ |  |

calculation the refinement converged at $R=0 \cdot 11$ after five more cycles. Throughout the refinement with anisotropic temperature factors to avoid 'yawing' and the consequent false minima, the parameters were altered by 0.3 of the calculated shift.

The form factors used were those in International Tables for X-ray Crystallography (1962). The observed structure amplitudes and structure factors calculated from the atomic parameters in Table 1 are available.*

[^1]A key to the labelling of the atoms produced by different symmetry operations is given in Table 2 and the interatomic distances and interbond angles are given in Table 3; water oxygens are labelled $W$ to distinguish them from acetate oxygen atoms. Fig. 1 shows a projection of the unit cell along the $c$ axis and Fig. 2 is a detail of the chain of coordination polyhedra viewed down the $a$ axis.

## Results and discussion

The structure contains four distinct water molecules, two in general positions which with two in special positions on the twofold axis produce the molecular formula $3 \mathrm{H}_{2} \mathrm{O}$. The coordination of the six closest oxygen atoms about the $\mathrm{Na}^{+}$ion is approximately octahedral (Table 3). It consists of one acetate oxygen atom and the four water molecules $W(1-4)$ with the final position occupied by a water molecule $\{W(2)[2]\}$ centrosymmetically related to that already used. Adjacent oxygen polyhedra share an edge through the atoms in special positions $[W(3)$ and $W(4)]$ on one side and through the centrosymmetically related pair of atoms $\{W(2)$ and $W(2)[2]\}$ on the other (Fig. 2). In the centre of the unit cell there is a tube of apparent free space but this is efficiently filled by the methyl groups of the acetate ion (Fig. 1), with several short carbon-carbon contact distances in the range 3.6 $3 \cdot 8 \AA$.

## Acetate ion

The two $\mathrm{C}-\mathrm{O}$ bond lengths are $1.23(013)$ and $1 \cdot 31$ (014) $\AA$ for atoms $\mathrm{O}(1)$ and $\mathrm{O}(2)$ respectively, so they are only just significantly different. In ammonium acetate the corresponding distances are 1.250 and $1 \cdot 253 \AA$ (Nahringbauer, 1967), while in lithium acetate dihydrate these distances are equivalent by symmetry with a length of $1.245 \AA$ (Galigné, Mouvet \& Falgueirettes, 1970). The disparity in the $\mathrm{C}-\mathrm{O}$ bond

Table 3. Interatomic distances $(\AA)$ and interbond angles $\left({ }^{\circ}\right)$
E.s.d.'s are in parentheses. Numbers in square brackets indicate the symmetry (see Table 2 ) and $W$ refers to the oxygen atom of a water molecule.


| $\mathrm{O}(1)[1]-\mathrm{Na}[1]-W(2)[2]$ | $98.5(3)$ |
| :--- | ---: |
| $\mathrm{O}(1)-\mathrm{Na}-W(1)$ | $104 \cdot 2(3)$ |
| $\mathrm{O}(1)-\mathrm{Na}-W(2)$ | $164.7(3)$ |
| $\mathrm{O}(1)-\mathrm{Na}-W(3)$ | $86.0(3)$ |
| $\mathrm{O}(1)-\mathrm{Na}-W(4)$ | $98.8(3)$ |
| $W(1)-\mathrm{Na}-W(2)$ | $90.6(3)$ |
| $W(1)[1]-\mathrm{Na}[1]-W(2)[2]$ | $80.9(3)$ |
| $W(1)-\mathrm{Na}-W(3)$ | $165.7(3)$ |
| $W(1)-\mathrm{Na}-W(4)$ | $95.7(3)$ |
| $W(2)-\mathrm{Na}-W(3)$ | $80.0(3)$ |
| $W(2)-\mathrm{Na}-W(4)$ | $75.9(3)$ |
| $W(2)[1]-\mathrm{Na}[1]-W(2)[2]$ | $87.1(3)$ |
| $W(2)[2]-\mathrm{Na}[1]-W(3)[1]$ | $87.9(3)$ |
| $W(2)[2]-\mathrm{Na}[1]-W(4)[1]$ | $162.6(3)$ |
| $W(3)-\mathrm{Na}-W(4)$ | $92.4(3)$ |

lengths in this compound is probably caused by hydrogen bonding, since each oxygen atom forms two hydrogen bonds but one, $\mathrm{O}(2) \cdots W(1)$, is somewhat stronger than the others. The conformation of methyl hydrogen atoms around the $\mathrm{C}-\mathrm{C}$ axis is such that the hydrogen atoms of one group fit into the spaces between the hydrogen atoms of an adjacent group.

## $\mathrm{Na}^{+}-\mathrm{O}$ contacts

The $\mathrm{Na}^{+}-\mathrm{O}$ are in the range 2.35 (1) to $2 \cdot 56$ (1) $\AA$ with the distance to the acetate oxygen atom in the middle of the range at 2.46 (1) $\AA$. The $\mathrm{O}-\mathrm{Na}^{+}-\mathrm{O}$ interbond angles vary between $80 \cdot 9$ (3) and $104 \cdot 2$ (3) ${ }^{\circ}$ for the angles which would be $90^{\circ}$ in a regular octahedron and $162 \cdot 6(3)-165 \cdot 7(3)^{\circ}$ for those angles that should be $180^{\circ}$. A similar distorted octahedron was found by Gupta \& Sahu (1970) in sodium hydrogen fumarate, where the $\mathrm{Na}^{+}-\mathrm{O}$ distances ranged from 2.38 to $2.64 \AA$, and by Young, Tollin \& Wilson (1974) indisodium deoxyguanosine-5'-phosphate tetrahydrate, where the $\mathrm{Na}^{+}-\mathrm{O}$ distances were between $2.354(5)$ and 2.559 (5) $\AA$ and the angles 78.1 (3) to $100 \cdot 1$ (3) ${ }^{\circ}$.

The separations between adjacent $\mathrm{Na}^{+}$ions are 3.39 and $3.56 \AA$ with the closer separation corresponding to the octahedra shared through atoms $W(3)$ and $W(4)$. In trisodium tetraaquooctacyanotungstate where there is a similar coordination arrangement with shared edges around the $\mathrm{Na}^{+}$ion the $\mathrm{Na}^{+} \ldots \mathrm{Na}^{+}$separations are 3.67 and $3.50 \AA$ (Bok, Leipoldt \& Basson, 1970).

## Hydrogen bonding

The dashed lines in Fig. 1 indicate the probable hydrogen-bonding scheme. The oxygen $\cdots$ oxygen contact distances for the hydrogen bonds are listed in Table 3. They vary between 2.68 and $2.96 \AA$. The $\mathrm{O}-\mathrm{H} \cdots \mathrm{O}$ angles are in the range $142-174^{\circ}$. The only hydrogen atom not involved in bonding is $\mathrm{H}(8)$ which
itself makes the closest contact to $\mathrm{O}(2)$ of $2 \cdot 3 \AA$. Each oxygen atom of the acetate ion forms two hydrogen bonds. The acetate ions related by the twofold screw axis are hydrogen bonded together through water molecule $W(1)$ and the system $\cdots W(1)[4] \cdots \mathrm{O}(2)-$ $\mathrm{C}(1)-\mathrm{O}(1) \cdots W(1)[6] \cdots \mathrm{O}(2)[7]-$ forms a helix about this axis. The helices are bonded together by hydrogen bonds involving $W(2), W(3)$ and $W(4)$.

Initial calculations were carried at the Atomic Energy Computing Centre, Dacca, using programs written by M.O.R., and the final calculations and refinement were computed at the University of Ulster Computing Centre using Cameron's (1972) CRYSTAL system. This work was a collaboration of crystallographers of the Universities of Dacca and Ulster. M.O.R. acknowledges the research grant of Dacca University and K.M.M. the travelling grant of the Nuffield Foundation.

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[^0]:    * On sabbatical leave as Nuffield Fellow, New University of Ulster.

[^1]:    * This table has been deposited with the British Library Lending Division as Supplementary Publication No. SUP 31123 (7 pp.). Copies may be obtained through The Exccutive Secretary, International Union of Crystallography, 13 White Friars, Chester CH1 1 NZ, England. Copies are also available from the Libraries of the University of Ulster, Coleraine, $N$. Ireland and the University of Dacca. Catalogue No. QD 921 C. 35. Copies may be obtained on application to the Librarian for Science.

